Simba: Efficient In-Memory Spatial Analytics

Dong Xie¹, Feifie Li¹, Bin Yao², Gefei Li², Liang Zhou¹, Minyi Guo²
¹University of Utah  ²Shanghai Jiao Tong University
{dongx, lifeifei}@cs.utah.edu {yaobin@cs., oizz01@, nichozl@, guo-my@cs.}sjtu.edu.cn

ABSTRACT

Large spatial data becomes ubiquitous. As a result, it is critical to provide fast, scalable, and high-throughput spatial queries and analytics for numerous applications in location-based services (LBS). Traditional spatial databases and spatial analytics systems are disk-based and optimized for IO efficiency. But increasingly, data are stored and processed in memory to achieve low latency, and CPU time becomes the new bottleneck. We present the Simba (Spatial In-Memory Big data Analytics) system that offers scalable and efficient in-memory spatial query processing and analytics for big spatial data. Simba is based on Spark and runs over a cluster of commodity machines. In particular, Simba extends the Spark SQL engine to support rich spatial queries and analytics through both SQL and the DataFrame API. It introduces indexes over RDDs in order to work with big spatial data and complex spatial operations. Lastly, Simba implements an efficient query optimizer, which leverages its indexes and novel spatial-aware optimizations, to achieve both low latency and high throughput. Extensive experiments over large data sets demonstrate Simba’s superior performance compared against other spatial analytics systems.

1. INTRODUCTION

There has been an explosion in the amount of spatial data in recent years. Mobile applications on smart phones and various internet of things (IoT) projects (e.g., sensor measurements for smart city) generate humongous volume of data with spatial dimensions. What’s more, spatial dimensions often play an important role in these applications, for example, user and driver locations are the most critical features for the Uber app. How to query and analyze such large spatial data with low latency and high throughput is a fundamental challenge. Most traditional and existing spatial databases and spatial analytics systems are disk-oriented (e.g., Oracle Spatial, SpatialHadoop, and Hadoop GIS [11, 22]). Since they have been optimized for IO efficiency, their performance often deteriorates when scaling to large spatial data.

A popular choice for achieving low latency and high throughput nowadays is to use in-memory computing over a cluster of commodity machines. Systems like Spark [38] have witnessed great success in big data processing, by offering low query latency and high analytical throughput using distributed memory storage and computing. Recently, Spark SQL [13] extends Spark with a SQL-like query interface and the DataFrame API to conduct relational processing on different underlying data sources (e.g., data from DFS). Such an extension provides useful abstraction for supporting easy and user-friendly big data analytics over a distributed memory space. Furthermore, the declarative nature of SQL also enables rich opportunities for query optimization while dramatically simplifying the job of an end user.

However, none of the existing distributed in-memory query and analytics engines, like Spark, Spark SQL, and MemSQL, provide native support for spatial queries and analytics. In order to use these systems to process large spatial data, one has to rely on UDFs or user programs. Since a UDF (or a user program) sits outside the query engine kernel, the underlying system is not able to optimize the workload, which often leads to very expensive query evaluation plans. For example, when Spark SQL implements a spatial join via UDF, it has to use the expensive cartesian product approach which is not scalable for large data.

Inspired by these observations, we design and implement the Simba (Spatial In-Memory Big data Analytics) system, which is a distributed in-memory analytics engine, to support spatial queries and analytics over big spatial data with the following main objectives: simple and expressive programming interfaces, low query latency, high analytics throughput, and excellent scalability. In particular, Simba has the following distinct features:

- Simba extends Spark SQL with a class of important spatial operations and offers simple and expressive programming interfaces for them in both SQL and DataFrame API.
- Simba supports (spatial) indexing over RDDs (resilient distributed dataset) to achieve low query latency.
- Simba designs a SQL context module that executes multiple spatial queries in parallel to improve analytical throughput.
- Simba introduces spatial-aware optimizations to both logical and physical optimizations, and uses cost-based optimizations (CBO) to select good spatial query plans.

Since Simba is based on Spark, it inherits and extends Spark’s fault tolerance mechanism. Different from Spark SQL that relies on UDFs to support spatial queries and analytics, Simba supports such operations natively with the help of its index support, query optimizer, and query evaluator. Because these modules are tailored towards spatial operations, Simba achieves excellent scalability in answering spatial queries and analytics over large spatial data.

The rest of the paper is organized as follows. We introduce the necessary background in Section 2 and provide a system overview of Simba in Section 3. Section 4 presents Simba’s programming interfaces, and Section 5 discusses its indexing support. Spatial operations in Simba are described in Section 6, while Section 7 explains
Simba’s query optimizer and fault tolerance mechanism. Extensive experimental results over large real data sets are presented in Section 8. Section 9 summarizes the related work in addition to those discussed in Section 2, and the paper is concluded in Section 10.

2. BACKGROUND AND RELATED SYSTEMS

2.1 Spark Overview

Apache Spark [38] is a general-purpose, widely-used cluster computing engine for big data processing, with APIs in Scala, Java and Python. Since its inception, a rich ecosystem based on Spark for in-memory big data analytics has been built, including libraries for streaming, graph processing, and machine learning [6].

Spark provides an efficient abstraction for in-memory cluster computing called Resilient Distributed Datasets (RDDs). Each RDD is a distributed collection of Java or Python objects partitioned across a cluster. Users can manipulate RDDs through the functional programming APIs (e.g., map, filter, reduce) provided by Spark, which take functions in the programming language and map them to other nodes on the cluster. For instance, we can count lines containing “ERROR” in a text file with the following Scala code:

```scala
lines = spark.textFile("hdfs://...")
errors = lines.filter(l => l.contains("ERROR"))
printin(errors.count())
```

This example creates an RDD of strings called `lines` by reading an HDFS file, and uses `filter` operation to obtain another RDD `errors` which consists of the lines containing “ERROR” only. Lastly, `count` is performed on `errors` for output.

RDDs are fault-tolerant as Spark can recover lost data using lineage graphs by rerunning operations to rebuild missing partitions. RDDs can also be cached in memory or made persistent on disk explicitly to accelerate data reusing and support iteration [38]. RDDs are evaluated lazily. Each RDD actually represents a “logical plan” to compute a dataset, which consists of one or more “transformations” on the original input RDD, rather than the physical, materialized data itself. Spark will wait until certain output operations (known as “action”), such as `collect`, to launch a computation. This allows the engine to do some simple optimizations, such as pipelining operations. Back to the example above, Spark will pipeline reading lines from the HDFS file with applying the filter and counting records. Thanks to this feature, Spark never needs to read the whole file to obtain the results. Though such optimization is extremely useful, it is also limited because the engine does not understand the structure of data in RDDs (that can be arbitrary Java/Python objects) or the semantics of user functions (which may contain arbitrary codes and logic).

2.2 Spark SQL Overview

Spark SQL [13] integrates relational processing with Spark’s functional programming API. Built with experience from its predecessor Shark [35], Spark SQL leverages the benefits of relational processing (e.g., declarative queries and optimized storage), and allows users to call other analytics libraries in Spark (e.g., SparkML for machine learning) through its DataFrame API.

Spark SQL can perform relational operations on both external data sources (e.g. JSON, Parquet [5] and Avro [4]) and Spark’s built-in distributed collections (i.e., RDDs). Meanwhile, it evaluates operations lazily to get more optimization opportunities. Spark SQL introduces a highly extensible optimizer called Catalyst, which makes it easy to add data sources, optimization rules, and data types for different application domains such as machine learning.

Spark SQL is a full-fledged query engine based on the underlying Spark core. It makes Spark accessible to a wider user base and offers powerful query execution and optimization planning. Despite the rich support of relational style processing, Spark SQL does not perform well on spatial queries over multi-dimensional data. Expressing spatial queries is inconvenient or even impossible. For instance, a relational query as below is needed to express a 10 nearest neighbor query for a query point \( q = (3.0, 2.0) \) from the table `point1` (that contains a set of 2D points):

```
SELECT * FROM point1
ORDERED BY (point1.x - 3.0) * (point1.x - 3.0) + (point1.y - 2.0) * (point1.y - 2.0)
LIMIT 10.
```

To make the matter worse, if we want to retrieve (or do analyses over) the intersection of results from multiple \( k \)NN queries, more complex expressions such as nested sub-queries will be involved. In addition, it is impossible to express a \( k \)NN join succinctly over two tables in a single Spark SQL query. Another important observation is that most operations in Spark SQL require scanning the entire RDDs. This is a big overhead since most computations may not actually contribute to the final results. Lastly, Spark SQL does not support optimizations for spatial analytics.

2.3 Cluster-Based Spatial Analytics Systems

There exists a number of systems that support spatial queries and analytics over distributed spatial data using a cluster of commodity machines. We will review them briefly next.

Hadoop based system. SpatialHadoop [22] is an extension of the MapReduce framework [18], based on Hadoop, with native support for spatial data. It enriches Hadoop with spatial data awareness in language, storage, MapReduce, and operation layers. In the language layer, it provides an extension to Pig [30], called Pigeon [21], which adds spatial data types, functions and operations as UDFs in Pig Latin Language. In the storage layer, SpatialHadoop adapts traditional spatial index structures, such as Grid, R-tree and R+-tree, to a two-level index framework. In the MapReduce layer, SpatialHadoop extends MapReduce API with two new components, `SpatialFileSplitter` and `SpatialRecordReader`, for efficient and scalable spatial data processing. In the operation layer, SpatialHadoop is equipped with several predefined spatial operations including box range queries, \( k \) nearest neighbor (\( k \)NN) queries and spatial joins over geometric objects using conditions such as `within` and `intersect`. However, only two-dimensional data is supported, and operations such as circle range queries and \( k \)NN joins are not supported as well (according to the latest open-sourced version of SpatialHadoop).

SpatialHadoop does have good support on different geometric objects, e.g. segments and polygons, and operations over them, e.g. generating convex hulls and skylines, which makes it a distributed geometric data analytics system over MapReduce [20].

Hadoop GIS [11] is a scalable and high performance spatial data warehousing system for running large scale spatial queries on Hadoop. It is available as a set of libraries for processing spatial queries and an integrated software package in Hive [33]. In its latest version, the SATO framework [34] has been adopted to provide different partition and indexing approaches. However, Hadoop GIS only supports data up to two dimensions and two query types: box range queries and spatial joins over geometric objects with predicates like `within` (within distance).

GeoSpark. GeoSpark [37] extends Spark for processing spatial data. It provides a new abstraction called Spatial Resilient Distributed Datasets (SRDDs) and a few spatial operations. GeoSpark supports range queries, \( k \)NN queries, and spatial joins over SRDDs. Besides, it allows an index (e.g. quad-trees and R-trees) to be the object inside each local RDD partition. Note that Spark allows developers to build RDDs over objects of any user-defined types outside Spark kernel. Thus essentially, an SRDD simply encapsu-
lates an RDD of spatial objects (which can be points, polygons or circles) with some common geometry operations (e.g. calculating the MBR of its elements). Moreover, even though GeoSpark is able to use index to accelerate query processing within each SRDD partition, it does not support flexible global index inside the kernel. GeoSpark only supports two-dimensional data, and more importantly, it can only deal with spatial coordinates and does not allow additional attributes in spatial objects (e.g. strings for description). In other words, GeoSpark is a library running on top of and outside Spark without a query engine. Thus, GeoSpark does not provide a user-friendly programming interface like SQL or the DataFrame API, and has neither query planner nor query optimizer.

**SpatialSpark.** SpatialSpark [36] implements a set of spatial operations for analyzing large spatial data with Apache Spark. Specifically, SpatialSpark supports range queries and spatial joins over geometric objects using conditions like intersect and within. SpatialSpark adopts data partition strategies like fixed grid or kd-tree on data files in HDF5 and builds an index (outside the Spark engine) to accelerate spatial operations. Nevertheless, SpatialSpark only supports two-dimensional data, and does not index RDDs natively. What’s more, same as GeoSpark, it is also a library running on top of and outside Spark without a query engine and does not support SQL and the DataFrame API.

**Remarks.** Note that all the systems mentioned above do not support concurrent queries natively with a multi-threading module. Thus, they have to rely on user-level processes to achieve this, which introduce non-trivial overheads from the operating system and hurt system throughput. In contrast, Simba employs a thread pool inside the query engine, which provides much better performance on concurrent queries. There are also systems like GeoMesa and MD-HBase that are related and reviewed in Section 9. Table 1 compares the core features between Simba and other systems.

### 2.4 Spatial Operations

In this paper, we focus on spatial operations over point objects. Our techniques and frameworks also support rectangular objects (such as MBRs), and can be easily extended to support general geometric objects. Table 2 lists the frequently used notations.

Formally, consider a data set \( R \subseteq \mathbb{R}^d \) with \( N \) records, where \( d \geq 1 \) is the dimensionality of the data set and each record \( r \in R \) is a point in \( \mathbb{R}^d \). For any two points \( p, q \in \mathbb{R}^d \), \( |p, q| \) denotes their \( L_2 \) distance. We consider the following spatial operations in this paper, due to their wide applications in practice [32].

**Definition 1 (Range Query)** Given a query area \( Q \) (either a rectangle or a circle) and a data set \( R \), a range query (denoted as \( \text{range}(Q, R) \)) asks for all records within \( Q \) from \( R \). Formally,

\[
\text{range}(Q, R) = \{ r | r \in R, r \in Q \}.
\]

**Definition 2 (kNN Query)** Given a query point \( q \in \mathbb{R}^d \), a data set \( R \) and an integer \( k \geq 1 \), the \( k \) nearest neighbors of \( q \) w.r.t. \( R \), denoted as \( \text{nn}(q, S) \), is a set of \( k \) records from \( R \) where

\[
\forall o \in \text{nn}(q, R), \forall r \in R - \text{nn}(q, R), |o, r| \leq |q, r|.
\]

**Definition 3 (Distance Join)** Given two data sets \( R \) and \( S \), and a distance threshold \( \tau > 0 \), the distance join between \( R \) and \( S \), denoted as \( R \bowtie_{\tau} S \), finds all pairs \( (r, s) \) within distance \( \tau \) such that \( r \in R \) and \( s \in S \). Formally,

\[
R \bowtie_{\tau} S = \{(r, s) | r \in R \times S, |r, s| \leq \tau\}.
\]

**Definition 4 (kNN Join)** Given two data sets \( R \) and \( S \), and an integer \( k \geq 1 \), the \( k \)NN join between \( R \) and \( S \), denoted as \( R \bowtie_{k\text{nn}} S \), pairs each object \( r \in R \) with each of its \( k \)NNs from \( S \). Formally,

\[
R \bowtie_{k\text{nn}} S = \{(r, s) | r \in R, s \in \text{nn}(r, S)\}.
\]

### 3. Simba ARCHITECTURE OVERVIEW

Simba builds on Spark SQL [13] and is optimized specially for large scale spatial queries and analytics over multi-dimensional data sets. Simba inherits and extends SQL and the DataFrame API, so that users can easily specify different spatial queries and analytics to interact with the underlying data. A major challenge in this process is to extend both SQL and the DataFrame API to support a rich class of spatial operations natively inside the Simba kernel.

Figure 1 shows the overall architecture of Simba. Simba follows a similar architecture as that of Spark SQL, but introduces new features and components across the system stack. In particular, new modules from different Spark SQL are highlighted by orange boxes in Figure 1. Similar to Spark SQL, Simba allows users to interact with the system through command line (CLI), JDB, and scala/python programs. It can connect to a wide variety of data sources, including those from HDF5 (Hadoop Distributed File System), relational databases, Hive, and native RDDs.

An important design choice in Simba is to stay outside the core spark engine and only introduce changes to the kernel of Spark SQL. This choice has made a few implementations more challenging (e.g. adding the support for spatial indexing without modifying Spark core), but it allows easy migration of Simba into new version of Spark to be released in the future.

**Programming interface.** Simba adds spatial keywords and grammar (e.g. POINT, RANGE, KNN, KNN JOIN, DISTANCE JOIN) in Spark SQL’s query parser, so that users can express spatial queries in SQL-like statements. We also extend the DataFrame API with a similar set of spatial operations, providing an alternative programming interface for the end users. The support of spatial operations

<table>
<thead>
<tr>
<th>Core Features</th>
<th>Simba</th>
<th>GeoSpark</th>
<th>SpatialSpark</th>
<th>SpatialHadoop</th>
<th>Hadoop ON</th>
<th>Notation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data dimensions</td>
<td>multiple</td>
<td>( d \leq 2 )</td>
<td>( d \leq 2 )</td>
<td>( d \leq 2 )</td>
<td>( d \leq 2 )</td>
<td>( R ) (resp. ( S ))</td>
<td>a table of a point set ( R ) (resp. ( S ))</td>
</tr>
<tr>
<td>SQL</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
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<td>(</td>
<td>r, s</td>
</tr>
<tr>
<td>Dataframe API</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{maxdist}(q, B) )</td>
<td>( \text{maxdist}(q, B) ) for point ( q ) and MBR ( B )</td>
</tr>
<tr>
<td>Spatial indexing</td>
<td>R-tree</td>
<td>R-tree</td>
<td>grid/kd-tree</td>
<td>grid/kd-tree</td>
<td>SATO</td>
<td>( \text{maxdist}(A, B) )</td>
<td>( \text{maxdist}(A, B) ) for MBRs ( A ) and ( B )</td>
</tr>
<tr>
<td>In-memory</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{mindist}(q, B) )</td>
<td>( \text{mindist}(q, B) ) for point ( q ) and MBR ( B )</td>
</tr>
<tr>
<td>Query planner</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{mindist}(A, B) )</td>
<td>( \text{mindist}(A, B) ) for MBRs ( A ) and ( B )</td>
</tr>
<tr>
<td>Query optimizer</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{range}(A, R) )</td>
<td>records from ( R ) within area ( A )</td>
</tr>
<tr>
<td>Concurrent query execution</td>
<td>thread pool in query engine</td>
<td>user-level process</td>
<td>user-level process</td>
<td>user-level process</td>
<td>user-level process</td>
<td>k nearest neighbors of ( r ) from ( S )</td>
<td>( R \bowtie_{\tau} S )</td>
</tr>
<tr>
<td>Box range query</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( R \bowtie_{\tau} S )</td>
<td>KNN join between ( R ) and ( S )</td>
</tr>
<tr>
<td>Circle range query</td>
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<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( R \bowtie_{\tau} S )</td>
<td>r-th (resp. j-th) partition of table ( R ) (resp. ( S ))</td>
</tr>
<tr>
<td>k nearest neighbor</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{mindist}(q, B) )</td>
<td>( \text{mindist}(q, B) ) for point ( q ) and MBR ( B )</td>
</tr>
<tr>
<td>Distance join</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{mindist}(A, B) )</td>
<td>( \text{mindist}(A, B) ) for MBRs ( A ) and ( B )</td>
</tr>
<tr>
<td>kNN join</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>( \text{mindist}(A, B) )</td>
<td>( \text{mindist}(A, B) ) for MBRs ( A ) and ( B )</td>
</tr>
<tr>
<td>Geometric object</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>centroid of ( B )</td>
<td>centroid of ( \text{mindist}(R) )</td>
</tr>
<tr>
<td>Compound query</td>
<td>✓</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>✗</td>
<td>max (</td>
<td>p, q</td>
</tr>
</tbody>
</table>

Table 1: Comparing Simba against other systems.
in DataFrame API also allows Simba to interact with other Spark components easily, such as MLlib, GraphX, and Spark Streaming. Lastly, we introduce index management commands to Simba’s programming interface, in a way which is similar to that in traditional RDBMS. We will describe Simba’s programming interface with more details in Section 4 and Appendix A.

**Indexing.** Spatial queries are expensive to process, especially for data in multi-dimensional space and complex operations like spatial joins and kNN. To achieve better query performance, Simba introduces the concept of indexing to its kernel. In particular, Simba implements several classic index structures including hash maps, tree maps, and R-trees [14, 23] over RDDs in Spark. Simba adopts a two-level indexing strategy, namely, local and global indexing. The global index collects statistics from each RDD partition and helps the system prune irrelevant partitions. Inside each RDD partition, local indexes are built to accelerate local query processing so as to avoid scanning over the entire partition. In Simba, user can build and drop indexes anytime on any table through index management commands. By the construction of a new abstraction called IndexRDD, which extends the standard RDD structure in Spark, indexes can be made persistent to disk and loaded back together with associated data to memory easily. We will describe the Simba’s indexing support in Section 5.

**Spatial operations.** Simba supports a number of popular spatial operations over point and rectangular objects. These spatial operations are implemented based on native Spark RDD API. Multiple access and evaluation paths are provided for each operation, so that the end users and Simba’s query optimizer have the freedom and opportunities to choose the most appropriate method. Section 6 discusses how various spatial operations are supported in Simba.

**Optimization.** Simba extends the Catalyst optimizer of Spark SQL and introduces a cost-based optimization (CBO) module that tailors towards optimizing spatial queries. The CBO module leverages the index support in Simba, and is able to optimize complex spatial queries to make the best use of existing indexes and statistics. Query optimization in Simba is presented in Section 7.

**Workflow in Simba.** Figure 2 shows the query processing workflow of Simba. Simba begins with a relation to be processed, either from an abstract syntax tree (AST) returned by the SQL parser or a DataFrame object constructed by the DataFrame API. In both cases, the relation may contain unresolved attribute references or relations. An attribute or a relation is called unresolved if we do not know its type or have not matched it to an input table. Simba resolves such attributes and relations using Catalyst rules and a Catalog object that tracks tables in all data sources to build logical plans. Then, the logical optimizer applies standard rule-based optimization, such as constant folding, predicate pushdown, and spatial-specific optimizations like distance pruning, to optimize the logical plan. In the physical planning phase, Simba takes a logical plan as input and generates one or more physical plans based on its spatial operation support as well as physical operators inherited from Spark SQL. It then applies cost-based optimizations based on existing indexes and statistics collected in both Cache Manager and Index Manager to select the most efficient plan. The physical planner also performs rule-based physical optimization, such as pipelining projections and filters into one Spark map operation. In addition, it can push operations from the logical plan into data sources that support predicate or projection pushdown. In Figure 2, we highlight the components and procedures where Simba extends Spark SQL with orange color.

Simba supports analytical jobs on various data sources such as CSV, JSON and Parquet [5]. Figure 3 shows how data are represented in Simba. Generally speaking, each data source will be transformed to an RDD of records (i.e., RDD[Row]) for further evaluation. Simba allows users to materialize (often referred as “cache”) hot data in memory using columnar storage, which can reduce memory footprint by an order of magnitude because it relies on columnar compression schemes such as dictionary encoding and run-length encoding. Besides, user can build various indexes (e.g. hash maps, tree maps, R-trees) over different data sets to accelerate interactive query processing.

**Novelty and contributions.** To the best of our knowledge, Simba is the first full-fledged (i.e., support SQL and DataFrame with a sophisticated query engine and query optimizer) in-memory spatial query and analytics engine over a cluster of machines. Even though our architecture is based on Spark SQL, achieving efficient and scalable spatial query parsing, spatial indexing, spatial query algorithms, and a spatial-aware query engine in an in-memory, distributed and parallel environment is still non-trivial, and requires significant design and implementation efforts, since Spark SQL is tailored to relational query processing. In summary,

- We propose a system architecture that adapts Spark SQL to support rich spatial queries and analytics.
- We design the two-level indexing framework and a new RDD abstraction in Spark to build spatial indexes over RDDs natively inside the engine.
- We give novel algorithms for executing spatial operators with efficiency and scalability, under the constraints posed by the RDD abstraction in a distributed and parallel environment.
- Leveraging the spatial index support, we introduce new logical and cost-based optimizations in a spatial-aware query optimizer; many such optimizations are not possible in Spark SQL due to the lack of support for spatial indexes. We also exploit partition tuning and query optimizations for specific spatial operations such as kNN joins.
4. PROGRAMMING INTERFACE

Simba offers two programming interfaces, SQL and the DataFrame API [13], so that users can easily express their analytical queries and integrate them into other components of the Spark ecosystem. Simba’s full programming interface is discussed in Appendix A.

Points. Simba introduces the point object in its engine, through a scala class. Users can express a multi-dimensional point using keyword POINT. Not only constants or attributes of tables, but also arbitrary arithmetic expressions can be used as the coordinates of points, e.g., `POINT(x + 2, y - 3, z * 2)` is a three-dimensional point with the first coordinate as the sum of attribute x’s value and constant 2. This enables flexible expression of spatial points in SQL. Simba will calculate each expression in the statement and wrap them as a point object for further processing.

Spatial predicates. Simba extends SQL with several new predicates to support spatial queries, such as RANGE for box range queries, CIRCULERANGE for circle range queries, and KNN for k nearest neighbor queries. For instance, users can ask for the 3-nearest neighbors of point (4, 5) from table point1 as below:

```sql
SELECT * FROM point1
WHERE POINT(x, y) IN KNN(POINT(4, 5), 3).
```

A box range query as follows asks for all points within the two-dimensional rectangle defined by point (10, 5) (lower left corner) and point (15, 8) (top right corner) from table point2:

```sql
SELECT * FROM point2
WHERE POINT(x, y) IN RANGE(POINT(10, 5), POINT(15, 8)).
```

Spatial joins. Simba supports two types of spatial joins: distance joins and kNN joins. Users can express these spatial joins in a θ-join like manner. Specifically, a 10-nearest neighbor join between two tables, `point1` and `point2`, can be expressed as:

```sql
SELECT * FROM point1 AS p1 JOIN point2 AS p2
ON POINT(p2.x, p2.y) IN KNN(POINT(p1.x, p1.y), 10).
```

A distance join with a distance threshold 20, between two tables `point3` and `point4` in three-dimensional space, is expressed as:

```sql
SELECT * FROM point3 AS p3 JOIN point4 AS p4
ON POINT(p4.x, p4.y, p4.z) IN CIRCULERANGE(POINT(p3.x, p3.y, p3.z), 20).
```

Index management. Users can manipulate indexes easily with index management commands introduced by Simba. For example, users can build an R-Tree index called `pointIndex` on attributes x, y, and z for table `sensor` using command:

```sql
CREATE INDEX pointIndex ON sensor(x, y, z) USE RTREE.
```

Compound queries. Note that Simba keeps the support for all grammars (including UDFs and UDTs) in Spark SQL. As a result, we can express compound spatial queries in a single SQL statement. For example, we can count the number of restaurants near a table using:

```sql
SELECT q.id, count(*) AS c
FROM pois AS q JOIN RESTS AS r
ON POINT(r.x, r.y) IN CIRCULERANGE(POINT(q.x, q.y), 10.0)
GROUP BY q.id ORDER BY c.
```

DataFrame support. In addition to SQL, users can also perform spatial operations over DataFrame objects using a domain-specific language (DSL) similar to data frames in R [10]. Simba’s DataFrame API supports all spatial operations extended to SQL described above. Naturally, all new operations are also compatible with the exiting ones from Spark SQL, which provides the same level flexibility as SQL. For instance, we can also express the last SQL query above in the following scala code:

```scala
pois.distanceJoin(rests, Point(poiss("x"), poiss("y")),
                   Point(rest("x"), rest("y")), 10.0)
        .groupBy(pois("id"))
        .agg(count("*").as("c").sort("c").show()).
```

5. INDEXING

Indexing is important for the efficient processing of spatial queries and analytics, especially for multi-dimensional data and complex spatial operations such as kNN and spatial joins. In particular, indexing is a critical component towards building an effective optimizer in Simba. Since Simba is an in-memory analytical engine, reducing disk I/Os is not a main focus of indexing. Rather, Simba leverages indexes to reduce query latency and improve query throughput via cutting down CPU costs. For example, indexing can help Simba prune irrelevant RDD partitions when processing a range query, which frees more CPU resources for the underlying Spark engine, leading to higher query throughput.

Simba builds (spatial) indexes directly over RDDs to speed up query processing. Specifically, tables are represented as RDDs of records (i.e., RDD[Row]). Thus, indexing records of a table becomes indexing elements in an RDD. However, RDDs are designed for sequential scan, thus random access is very expensive as it may become a full scan on the RDD. An extra complexity is that we want to introduce indexing support without changing the Spark core for the reasons explained in Section 3. To overcome these challenges, we change the storage format of an indexed table by introducing a new abstraction called IndexRDD[Row], and employ a two-level indexing strategy which can accommodate various index structures to support different queries in Simba.

IndexRDD. Recall that records from a table are stored as Row objects (Row objects), and each tables is stored as a RDD of Row that contains multiple partitions. To add index support over a table, we pack all records (i.e., Row objects) within an RDD partition into an array, which gives each record a unique subscript as its index. Such change makes random access inside RDD partitions an efficient operation with O(1) cost. To achieve this in Simba, we introduce the IPartition data structure as below:

```scala
case class IPartition[Type](Data: Array[Type], I: Index) Index is an abstract class that we have designed, and can be instantiated as: HashMap (a hash index), TreeMap (a one-dimensional index), and RTree (a multi-dimensional index). IndexRDD[Row] is simply defined as RDD[IPartition[Row]] by setting Type = Row in the following type declaration:
```

```scala
type IndexRDD[Type] = RDD[IPartition[Type]]
```

Records from a table are partitioned by a partitioner (that will be described next), and then packed into a set of IPartition objects. Since we pack all records within a partition to an array object inside IPartition, Simba does introduce small space overhead which may slow down table scanning operation compared to Spark SQL’s in-memory columnar storage and the original RDD[Row] structure. Experiments in Appendix D.3 have validated that the overhead of our design is insignificant.

Each IPartition object contains a local index over the records in that partition. Furthermore, each IPartition object emits the partition boundary information to construct a global index. In general, index construction in Simba consists of three phases: partition, local index, and global index, as shown in Figure 4.

Partition. In the partition phase, Simba partitions the input table (i.e., RDD[Row]) according to three main concerns: (1) Partition Size. Each partition should have a proper size so as to avoid memory overflow. (2) Data Locality. Records that locate close to each other (with respect to the indexing attributes) should be assigned to the same partition. (3) Load Balancing. Partitions should be roughly of the same size.

Spark allows users to define their own partition strategies by implementing an abstract class called Partitioner. A customized partitioner should specify how many partitions it will generate and how an element maps to a partition ID according to its partition
key. Spark provides two predefined partitioners, range partitioner and hash partitioner, which is sufficient when the partition key is one-dimensional, but does not fit well to multi-dimensional cases.

To address this problem, we have defined a new partitioner named STRPartitioner in Simba. STRPartitioner takes a set of random samples from the input table and runs the first iteration of Sort-Tile-Recursive (STR) algorithm [26] to determine partition boundaries. Note that the boundaries generated by the STR algorithm are minimum bounded rectangles (MBRs) of the samples. Thus, we need to extend these MBRs so that they can properly cover the space of the original data set. Finally, according to these extended boundaries, STRPartitioner specifies which partition each record belongs to.

Simba makes no restriction on partition strategies. Instead of using STRPartitioner, an end user can always supply his/her own partitioner to Simba. We choose STRPartitioner as the default partitioner of Simba due to its simplicity and proven effectiveness by existing studies [19]. As shown in Figure 4, we assume the input table \( R \) is partitioned into a set of partitions \( \{ R_1, \ldots, R_m \} \) by the partitioner. The number of partitions, \( m \), is determined by Simba’s optimizer which will be discussed in Section 7.

**Local index.** In this phase, Simba builds a user-specified index (e.g., R-tree) over data in each partition \( R_i \) as its local index. It also alters the storage format of the input table from RDD [Row] to IndexRDD [Row], by converting each RDD partition \( R_i \) to an IPartition [Row] object, as shown in Figure 4.

Specifically, for each partition \( R_i \), records are packed into an Array [Row] object. Then, Simba builds a local index over this Array [Row], and co-locates them in the IPartition [Row] object. As we can see, the storage format of the input table is no longer an RDD of objects, but an RDD of IPartition [Row] objects, which is an IndexRDD of Row objects by the definition above. While packing partition data and building local indexes, Simba also collects several statistics from each partition, such as the number of records and the partition boundaries, to facilitate the construction of the global index as illustrated in Figure 4.

**Global index.** The last phase of index construction is to build a global index which indexes all partitions. The global index enables us to prune irrelevant partitions for an input query without invoking many executors to look at data stored in different partitions.

In this phase, partition boundaries generated by the partitioner and other statistics collected in the local index phase are sent to the master node. Such information is utilized to bulk load an in-memory index, which is stored in the driver program on the master node. Users can specify different types of global indexes: When indexing one-dimensional data, a sorted array of the range boundaries is sufficient (the record count and other statistics for each partition are also stored in each array element). In multi-dimensional cases, more complex index structures, such as R-tree [14, 23] or KD-tree, can be used. By default, Simba keeps the global indexes for different tables in the memory of the master node at all time (i.e., in its

![Figure 4: Two-level indexing strategy in Simba.](image1)

![Figure 5: Pruning bound for RNN query at global index.](image2)
Global index returns the partition IDs whose MBRs intersect with the circle centered at \( q \) with radius \( \gamma \). Simba marks these partitions using `PartitionPruningRDD` and invokes local \( kNN \) queries using the aforementioned observation (1). Finally, it merges the \( k \) candidates from each of such partitions and takes the \( k \) records with minimum distances to \( q \) using RDD action `takeOrdered`.

### 6.2 Distance Join

Distance join is a \( \theta \)-join between two tables. Hence, we can express a distance join \( R \bowtie_{\text{mindist}(\tau)} S \) in Spark SQL as:

\[
\text{SELECT} \quad \text{FROM} \quad R \text{ JOIN } S \\
\text{ON} \quad (R.x - S.x) \times (R.x - S.x) + (R.y - S.y) \times (R.y - S.y) \leq 10.0 \times 10.0
\]

Spark SQL has to use the Cartesian product of two input tables for processing \( \theta \)-joins. It then filters from the Cartesian product based on the join predicates. Producing the Cartesian product is rather costly in Spark: If two tables are roughly of the same size, it leads to \( O(n^2) \) cost when each table has \( n \) partitions.

Most systems reviewed in Section 2 did not study distance joins. Rather, they used `spatial joins`: it takes two tables \( R \) and \( S \) (each is a set of geometric objects such as polygons), and a spatial join predicate \( \theta \) (e.g., overlaps, contains) as input, and returns the set of all pairs \( (r,s) \) such that \( \exists r \in R, \exists s \in S \) such that \( \theta(r,s) \) is true. \( \theta(r,s) \) is evaluated as object \( r \) overlaps object \( s \).

That said, we design the DJSpark algorithm in Simba for distance joins. DJSpark consists of three steps: data partition, global join, and local join, as shown in Figure 6.

#### 6.2.1 Data partition

Data partition phase is to partition \( R \) and \( S \) so as to preserve data locality where records that are close to each other are likely to end up in the same partition. We also need to consider partition size and load balancing issues. Therefore, we can re-use the `STRPartitioner` introduced in Section 5. The main difference is how we decide the partition size for \( R \) and \( S \). Simba has to ensure that it can keep two partitions (one from \( R \) and one from \( S \)) rather than one (when handling single-relation operations like range queries) in executors’ heap memory at the same time.

Note that the data partition phase can be skipped for \( R \) (or \( S \)) if \( R \) (or \( S \)) has been already indexed.

#### 6.2.2 Global join

Given the partitions of table \( R \) and table \( S \), this step produces all pairs \((i,j)\) which may contribute any pair \((r,s)\) such that \( r \in R_i, s \in S_j, \) and \( |r| \leq \tau \). Note that for each record \( s \in S, s \) matches with some records in \( R \) only if \( \text{mindist}(s, R_i) \leq \tau \). Thus, Simba only needs to produce the pairs \((i,j)\) such that \( \text{mindist}(R_i, S_j) \leq \tau \). After generating these candidate pairs of partition IDs, Simba produces a combined partition \( P = \{R_i, S_j\} \) for each pair \((i,j)\). Then, these combined partitions are sent to workers for processing local joins in parallel.

#### 6.2.3 Local join

Given a combined partition \( P = \{R_i, S_j\} \) from the global join, local join builds a local index over \( S_j \) on the fly if \( S \) is not already indexed. For each record \( r \in R_i \), Simba finds all \( s \in S_j \) such that \( |r| \leq \tau \) by issuing a circle range query centered at \( r \) over the local index on \( S_j \).

### 6.3 \( kNN \) join

Several solutions [27,39] for \( kNN \) join were proposed on MapReduce. In Simba, we have redesigned and implemented these methods with the RDD abstraction of Spark. Furthermore, we design a new hash-join like algorithm, which shows the best performance.

#### 6.3.1 Baseline methods

The most straightforward approach is the `BKJSpark-N` method (block nested loop \( kNN \) join in Spark).

**Producing buckets.** \( R \) (and \( S \)) is divided into \( n_1 \) (\( n_2 \)) equal-sized blocks, which simply puts every \( \{R_1/n_1 \text{ or } S_1/n_2 \} \) records into a block. Next, every pair of blocks, i.e., \( (R_i, S_j) \) for \( i \in [1, n_1], j \in [1, n_2] \), are shuffled to a bucket (so a total of \( n_1 n_2 \) buckets).

**Local \( kNN \) join.** Buckets are processed in parallel. Within each bucket \( (R_i, S_j) \), Simba performs \( \text{knn}(r, S_j) \) for every \( r \in R_i \) through a nested loop over \( R_i \) and \( S_j \).

**Merge.** This step finds the global \( kNN \) of every \( r \in R \) among its \( n_2 k \) local \( kNN \) founds in the last step (a total of \( |R| n_2 k \) candidates). Simba runs `reduceByKey` (where the key is a record in \( R \)) in parallel to get the global \( kNN \) of each record in \( R \).

A simple improvement is to build a local R-tree index over \( S_j \) for every bucket \( (R_i, S_j) \), and use the R-tree for local \( kNN \) joins. We denoted it as `BKJSpark-R` (block R-tree \( kNN \) join in Spark).

#### 6.3.2 Voronoi \( kNN \) Join and z-Value \( kNN \) Join

The baseline methods need to check roughly \( n^2 \) buckets (when \( O(n_1) \approx O(n_2) \approx O(n) \)), which is expensive for both computation and communication in distributed systems. A MapReduce algorithm leveraging a Voronoi diagram based partitioning strategy was proposed in [27]. It executes only \( n \) local joins by partitioning both \( R \) and \( S \) into \( n \) partitions respectively, where the partition strategy is based on the Voronoi diagram for a set of pivot points selected from \( R \). In Simba, We adapt this approach and denote it as the VKJSpark method (Voronoi \( kNN \) join in Spark).

Another MapReduce based algorithm for \( kNN \) join was proposed in [39], which exploits \( z \)-values to map multi-dimensional points into one dimension and uses random shift to preserve spatial locality. This approach also produces \( n \) partitions for \( R \) and \( S \) respectively, such that for any \( r \in R_i \) and \( i \in [1, n] \), \( \text{knn}(r, S) \subseteq \text{knn}(r, S_i) \) with high probability. Thus, it is able to provide high quality approximations using only \( n \) local joins. The partition step is much simpler than the Voronoi \( kNN \) join, but it only provides approximate results and there is an extra cost for producing exact results in a post-processing step. We adapt this approach in Simba, and denote it as the ZKJSpark method (z-value \( kNN \) join in Spark).

#### 6.3.3 R-Tree \( kNN \) Join

We leverage indexes in Simba to design a simpler yet more efficient method, the RKJSpark method (R-tree \( kNN \) join in Spark).

RKJSpark partitions \( R \) into \( n \) partitions \( \{R_1, \ldots, R_n\} \) using the STR partitioning strategy (as introduced in Section 5), which leads to balanced partitions and preserves spatial locality. It then takes a set of random samples \( S' \) from \( S \), and builds an R-tree \( T \) over \( S' \) in the driver program on the master node.

The key idea in RKJSpark is to derive a distance bound \( \gamma_i \) for each \( R_i \), so that we can use \( \gamma_i, R_i, T \) and find a subset \( S_i \subseteq S \) such that for any \( r \in R_i \), \( \text{knn}(r, S) \approx \text{knn}(r, S_i) \). This partitioning strategy ensures that \( \forall S \in \{R_1 \cup \ldots \cup R_n\} \), \( \text{knn}(r, S) \approx \text{knn}(r, \text{local } S_i) \), and allows the parallel execution of only \( n \) local \( kNN \) joins (on each \( R_i, S_i \) pair for \( i \in [1, n] \)).
(i.e., \( u_i = \max_{r \in R_i} |r, c_{r_i}| \)) in parallel. Simba collects these \( u_i \) values and centroids in the driver program on the master node.

Next, Simba finds \( \text{knn}(c_{r_i}, S) \) using the R-tree \( T \) for \( i \in [1, n] \). Without loss of generality, suppose \( \text{knn}(c_{r_i}, S) = \{s_1, \ldots, s_k\} \) (in ascending order of their distances to \( c_{r_i} \)). Finally, Simba sets:

\[
\gamma_i = 2u_i + |c_{r_i}, s_k| \text{ for partition } R_i,
\]

and finds \( S_i = \{s | s \in S, |c_{r_i}, s| \leq \gamma_i\} \) using a circle range query centered at \( c_{r_i} \) with radius \( \gamma_i \) over \( S \). This guarantees the desired property described above, due to:

**Theorem 1** For any partition \( R_i \), where \( i \in [1, n] \), we have:

\[
\forall r \in R_i; \text{knn}(r, S) \subseteq \{s | s \in S, |c_{r_i}, s| \leq \gamma_i\}, \text{ for } \gamma_i \text{ defined in} \ (1).
\]

The proof is shown in Appendix C. This leads to the design of RKJSpark. Specifically, for every \( s \in S \), RKJSpark includes a copy of \( s \) in \( S_i \) if \( |c_{r_i}, s| \leq \gamma_i \). Theorem 1 guarantees that for any \( r \in R_i \), \( \text{knn}(r, S) = \text{knn}(r, S_i) \).

Then, Simba invokes a zipPartitions operation for each \( i \in [1, n] \) to place \( R_i \) and \( S_i \) together into one combined RDD partition. In parallel, on each combined RDD partition, Simba builds an R-tree over \( S_i \) and executes a local \( k\text{NN} \) join by querying each record from \( R_i \) over this tree. The union of these \( n \) outputs is the final answer for \( R \text{knn} S \).

7. OPTIMIZER AND FAULT TOLERANCE

7.1 Query Optimization

Simba tunes system configurations and optimizes complex spatial queries automatically to make the best use of existing indexes and statistics. We employed a cost model for determining a proper number of partitions in different query plans. We also add new logical optimization rules and cost-based optimizations to the Catalyst optimizer and the physical planner of Spark SQL.

The number of partitions plays an important role in performance tuning for Spark. A good choice on the number of partitions not only guarantees no crashes caused by memory overflow, but also improves system throughput and reduces query latency. Given the memory available on a slave node in the cluster and the input table size, Simba partitions the table so that each partition can fit into the memory of a slave node and has roughly equal number of records so as to ensure load balancing in the cluster.

Simba builds a cost model to estimate the partition size under a given schema. It handles two cases: tables with fixed-length records and tables with variable-length records. The first case is easy and we omit its details. The case for variable-length record is much harder, since it is difficult to estimate the size of a partition even if we know how many records are going into a partition. Simba resolves this challenge using a sampling based approach, i.e., a small set of samples (using sampling without replacement) is taken to build estimators for estimating the size of different partitions, where the sampling probability of a record is proportional to its length. This is a coarse estimation depending on the sampling rate, but it is possible to formally analyze the performance of this estimator with respect to a given partitioning strategy, and in practice, this sampling approach is quite effective.

Using the cost model and a specified partition strategy, Simba then computes a good value for the number of partitions such that: 1) partitions are balanced in size; 2) size of each partition fits the memory size of a worker node; and 3) the total number of partitions is proportional to the number of workers in the cluster. Note that the size of different partitions should be close but not greater than a threshold, which indicates how much heap memory Spark can reserve for query processing. In Spark, on each slave node, a fraction of memory is reserved for RDD caching, which is specified as a system configuration \( \text{spark.storage.memoryFraction} \)
selectivity estimation (we maintain a count at each R-tree node \( u \) that is the number of leaf level entries covered by the subtree rooted at \( u \), and assume uniform distribution in each MBR for the purpose of selectivity estimation, ). Selectivity estimation for other types of predicates can be similarly made using top levels of local indexes.

CBO is also used for joins in Simba. When one of the tables to be joined is small (much smaller than the other table), Simba’s optimizer will switch to broadcast join, which skips the data partition phase on the small table and broadcasts it to every partition of the large table to do local joins. For example, if \( R \) is small and \( S \) is big, Simba does local joins over \((R, S_1), \ldots, (R, S_m)\). This optimization can be applied to both distance and \( kNN \) joins.

For \( kNN \) joins in particular, CBO is used to tune RKJSpark. We increase the sampling rate used to generate \( S' \) and/or partition table \( R \) with finer granularity to get a tighter bound for \( \gamma_i \). Simba’s optimizer adjusts the sampling rate of \( S' \) according to the master node’s memory size (and the max possible query value \( k_{\text{max}} \) so that \(|S'| > k_{\text{max}}; k \) is small for most \( kNN \) queries). Simba’s optimizer can also invoke another STR partitioner within each partition to get partition boundaries locally on each worker with finer granularity without changing the global partition and physical data distribution. This allows RKJSpark to compute tighter bounds of \( \gamma_i \) using the refined partition boundaries, thus reduces the size of \( S_i \).

Lastly, Simba implements a thread-safe SQL context (by creating thread-local instances for conflict components) to support the concurrent execution of multiple queries. Hence, multiple users can issue their queries concurrently to the same Simba instance.

7.2 Fault Tolerance

Simba’s fault tolerance mechanism extends that of Spark and Spark SQL. By the construction of IndexRDD, table records and local indexes in Simba are still encapsulated in RDD objects! They are persisted at the storage level of MEM_AND_DISK_SER, thus are naturally fault tolerant because of the RDD abstraction of Spark.

Any lost data (records or local indexes) will be automatically recovered by RDD’s fault tolerance mechanism (based on the lineage graph). Thus, Simba can tolerate any worker node failures at the same level that Spark provides. This also allows local indexes to be reused when data are loaded back into memory from disk, and avoids repartitioning and rebuilding of local indexes.

For the fault tolerance of the master node (or the driver program), Simba adopts the following mechanism. A Spark cluster can have multiple masters managed by zookeeper [7]. One will be elected “leader” and the others will remain in standby mode. If current leader fails, another master will be elected, recover the old master’s state, and then continue scheduling. Such mechanism would recover all system states and global indexes that reside in the driver program, thus ensures that Simba can survive after a master failure.

In addition, user can also choose to persist IndexRDD and global indexes to the file system, and have the option of loading them back from the disk. This enables Simba to load constructed index structures back to the system even after power failures.

Lastly, note that all user queries (including spatial operators) in Simba will be scheduled as RDD transformations and actions in Spark. Therefore, fault tolerance for query processing is naturally guaranteed by the underlying lineage graph fault tolerance mechanism provided in Spark kernel and consensus model of zookeeper.

8. EXPERIMENT

8.1 Experiment Setup

All experiments were conducted on a cluster consisting of 10 nodes with two configurations: (1) 8 machines with a 6-core Intel Xeon E5-2603 v3 1.60GHz processor and 20GB RAM; (2) 2 machines with a 6-core Intel Xeon E5-2620 2.00GHz processor and 56GB RAM. Each node is connected to a Gigabit Ethernet switch and runs Ubuntu 14.04.2 LTS with Hadoop 2.4.1 and Spark 1.3.0. We select one machine of type (2) as the master node and the rest are slave nodes. The Spark cluster is deployed in standalone mode. Our cluster configuration reserved up to 180GB of main memory for Spark. We used the following real and synthetic datasets:

- OSM is extracted from OpenStreetMap [9]. The full OSM data contains 2.2 billion records in 132GB, where each record has a record ID, a two-dimensional coordinate, and two text information fields (with variable lengths). We took uniform random samples of various sizes from the full OSM, and also duplicated the full OSM to get a data set \( 2 \times \text{OSM} \). These data sets range from 1 million to 4.4 billion records, with raw data size up to 264GB (in \( 2 \times \text{OSM} \)).

- GDELT stands for Global Data on Events, Language and Tone [8], which is an open database containing 75 million records in total. In our experiment, each record has 7 attributes: a timestamp and its spatial coordinates.

For single-relations operations (i.e. range and \( kNN \) queries), we evaluate the performance using throughput and latency. In particular, for both Simba and Spark SQL, we start a thread pool of size 10 in the driver program, and issue 500 queries to the system to calculate query throughput. For other systems that we reviewed in Section 2, since they do not have a multi-threading module, we submit 20 queries at the same time and run them as 20 different processes to ensure full utilization of the cluster resources. The throughput is calculated by dividing the total number of queries over the running time. Note that this follows the same way these systems had used to measure their throughput [22]. For all systems, we used 100 randomly generated queries to measure the average query latency. For join operations, we focus on the average running time of 10 randomly generated join queries for all systems.

In all experiments, HDFS block size is 64MB. By default, \( k = 10 \) for a \( kNN \) query or a \( kNN \) join. A range query is characterized by its query area, which is a percentage over the entire area where data locate. The default query area for range queries is 0.01%. The default distance threshold \( r \) for a distance join is set to 5 (each dimension is normalized into a domain from 0 to 1000). The default partition size is \( 500 \times 10^3 \) (500k) records per partition for single-relation operations and \( 30 \times 10^3 \) (30k) records per partition for join operations. The default data set size for single-relation operations is 500 million records on OSM data sets and 700 million on RC data sets. For join operations, the default data size is set to 3 million records in each input table. The default dimensionality is 2.

8.2 Cost of Indexing

We first investigate the cost of indexing in Simba and other distributed spatial analytics systems, including GeoSpark [37], SpatialSpark [36], SpatialHadoop [22], Hadoop GIS [11], and Geo-OMesa [24]. A commercial single-node parallel spatial database system (denoted as DBMS X) running on our master node is also included. Figure 8(a) presents the index construction time of different systems on the OSM data set when the data size varies from 30 million to 4.4 billion records (i.e., up to \( 2 \times \text{OSM} \)). Note that DBMS X took too much time when building an R-tree index over 4.4 billion records in \( 2 \times \text{OSM} \); hence its last point is omitted.
Simba and GeoSpark show the best index construction time, and both scale linearly to the data size. For example, Simba builds its index (which uses R-tree for both local indexes and the global index) over 1 billion records (60GB in file size) in around 25 minutes, which is 2.5x faster than SpatialHadoop, 3x faster than SpatialSpark, 12x faster than Hadoop GIS, and 15x faster than Geomesa. GeoSpark is slightly faster than Simba in building its indexes, because it uses a sampling partition strategy and it only builds a local index for each partition without building global indexes. Simba indexes RDDS natively, while Hadoop builds systems index HDFS file blocks. Even though SpatialSpark is also based on Spark, it indexes HDFS files rather than native RDDS. Geomesa builds a hash based index over Apache Accumulo.

We then investigated Simba’s indexing support in higher dimensions. Figure 8(b) shows the index construction time in Simba against number of dimensions on the RC data set. The cost increases linearly with the increase in dimensionality. Note that all other systems can only support up to two dimensions.

Next, we investigate the storage overhead (memory footprint or disk space used) of indexes in different systems, using OSM data of various sizes. Since Geomesa utilizes a hash based indexing strategy without global indexing, and DBMS X constructs its spatial index on a single node, we show their results with the local index size of the other systems in Figure 9(a), as local indexes dominate the index size of indexing in distributed systems. As a reference, we included the total size of all indexed keys (i.e., spatial coordinates) in Figure 9(a), denoted as “Raw Index Key”. SpatialSpark was not included in Figure 9(a) since local indexes are not supported.

As shown in Figure 9(a), Simba, SpatialHadoop and Hadoop GIS have the lowest storage overhead in their local indexes, while those of GeoSpark, Geomesa and DBMS X are much higher (roughly 4-5x). Global indexing is only supported by Simba, SpatialSpark, SpatialHadoop and Hadoop GIS. As shown in Figure 9(b), all systems have small global index storage overhead (only in the order of KB). In particular, the global index size in Simba is very small, which can easily fit in the memory of the master node. For example, it only consumes 653KB for the largest dataset (4.4 billion records with 264GB in raw data) in Simba. This is because that the number of partitions is not a large number (in the order of hundreds to tens of thousands) even for very large data.

Overall, Simba’s index storage overhead is acceptable, for example, for 1×OSM with 2.2 billion indexed keys, Simba’s local indexes use only 67GB, and its global index uses only 323KB, while the raw key size is about 40GB and the data itself is 132GB.

8.3 Comparison with Existing Systems

In this section, we tested different systems using various spatial operations with the default settings described in Section 8.1 over the 0.25× OSM data set (500 million records). A red cross mark in the following bar charts indicates the corresponding operation is not supported in a system.

Figure 10 shows the performance of single-relatioon operations on both range and kNN queries. Simba achieves 5-100x better performance (on both throughput and latency) than other existing cluster-based spatial analytics systems and the single-node parallel spatial database. Only DBMS X has outperformed Simba on kNN queries, as when k is small a single-node approach with index support is very efficient for finding kNNs. But its range query performance is worse than Simba.

Note that the performance of GeoSpark in this case is even worse than Hadoop based systems because GeoSpark has not utilized global indexes for query processing, which can help pruning large numbers of useless partitions (more than 90%) before scanning them.

For join operations (using 3 million records in each table), as shown in Figure 11, Simba runs distance join 1.5x faster than SpatialSpark, 25x faster than Hadoop GIS, and 26x faster than DBMS X. Note that distance join over point objects is not natively supported in SpatialHadoop. Nevertheless, SpatialHadoop supports spatial joins over geometric objects. We use \( RC(\tau/2) \) to express the number of useless partitions before scanning them.

In this section, we tested different systems using various spatial operations with the default settings described in Section 8.1 over the 0.25× OSM data set (500 million records). A red cross mark in the following bar charts indicates the corresponding operation is not supported in a system.

Figure 10 shows the performance of single-relatioon operations on both range and kNN queries. Simba achieves 5-100x better performance (on both throughput and latency) than other existing cluster-based spatial analytics systems and the single-node parallel spatial database. Only DBMS X has outperformed Simba on kNN queries, as when k is small a single-node approach with index support is very efficient for finding kNNs. But its range query performance is worse than Simba.

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Simba is also much more user-friendly with the native support on both SQL and the DataFrame API over both spatial and non-spatial operations within a single query, which are not supported by other systems (except that SpatialHadoop supports a SQL-like query language Pigeon). Simba is a full-fledged query engine with native support for query planning, query optimization, and concurrent query processing through thread pooling. Whereas, GeoSpark and SpatialSpark are user programs running on top of Spark (i.e., Spark libraries). What’s more, all these systems can only support up to two dimensions. Hence, in the following, we focus on comparing Simba with Spark SQL, which is also a full fledged analytics engine based on Spark but without native support for spatial operations, to see the benefit of extending Spark SQL to Simba for spatial analytics. We support various spatial operations in Spark SQL by directly expressing a spatial operation in its standard SQL syntax if it is possible, or using UDFs in SQL when it is not possible.

### 8.4 Comparison against Spark SQL

In this comparison we assume that tables are pre-loaded (i.e., we excluded the time of loading tables in both Simba and Spark SQL). **Range queries.** Figure 12 shows the performance of range queries in both engines using the OSM data set. Queries are centered at random points sampled from the input data. As a result, the query workload fits well to the distribution of the data, where dense areas will be queried with higher probabilities.

Figure 12(a) shows that Simba outperforms Spark SQL by about one order of magnitude on both query throughput and query latency when data size increases from 30 million to 4.4 billion records (2× OSM). The performance of both Simba and Spark SQL drops when the data size increases while that of Simba drops much slower, which implies Simba has much better scalability. This is due to the spatial index pruning and spatial-aware optimizations in Simba: larger data size does lead to more partitions to process and larger output size, but it also brings more pruning and optimization opportunities for its indexes and optimizer. In contrast, Spark SQL has to scan the whole table regardless.

Figure 12(b) shows how throughput and latency are influenced by the size of the query area. As the query area enlarges, performance of Simba becomes closer to that of Spark SQL. The reason for this is the result size becomes so large that there are less optimization opportunities for Simba’s query optimizer. Spark SQL has to scan the whole table regardless.

**kNN queries.** Figure 13 shows the performance of kNN queries on Spark SQL and Simba over the OSM data set, where query points are also randomly sampled from the input data as range queries.

![Figure 12: Range query performance on OSM.](image)

![Figure 13: kNN query performance on OSM.](image)
single SQL statement. One has to union $N$ SQL statements where $N$ is the number of records in the first input table, which is clearly not a practical solution for large tables. Hence, we focused on comparing different $k$NN join algorithms in Simba.

Figure 15 shows the performance over OSM data (default is 3 million records in each input table and $k = 10$). Clearly, RKJSpark shows the best performance and the best scalability (w.r.t. both data size and $k$). As an example, for a $k$NN join between two tables with 5 million records, RKJSpark join is 3x faster than VKJSpark and 70x faster than BKJSpark-R. Note that BKJSpark-R strictly dominates BKJSpark-N, hence, the latter is omitted.

Remarks. Spark still works when the dataset does not fit in main memory due to its disk persistence mechanism, Simba still has reasonable performance when data does not fit in memory. Clearly, performance will hurt in this case, but in principle, as long as each individual partition can fit in the heap memory of an executor, Spark is able to handle it, so is Simba (and its indexing support is even more important in these cases).

8.5 Support for Multi-Dimensions

In this section, we evaluate the performance of Simba and Spark SQL when handling data in higher dimensions. Note that other spatial analytics systems (GeoSpark, SpatialSpark, SpatialHadoop, and Hadoop GIS) do not support more than two dimensions.

For single-relation operations, as shown in Figures 16 and 17, both Simba and Spark SQL shows higher query latency and lower system throughput on the GDELT data set, as dimensionality increases from 2 to 6. Nevertheless, Simba outperforms Spark SQL by 1-2 orders of magnitude in all cases.

Figure 18 shows the impact of dimensionality on different join algorithms in Simba, by joining two tables with 3 million records from the RC data set as dimensionality goes from 2 to 6. DJSpark and RKJSpark remain the best performance in all dimensions.

9. RELATED WORK

We have already reviewed the most closely related systems in Sections 2 and 8, which Simba has significantly outperformed.

In addition, MD-HBase [29] extends HBase to support location services. It adds KD-tree and quad-tree indexes to HBase to support range and $k$NN queries. GeoMesa [24] builds a distributed spatial-temporal database on top of Apache Accumulo [3]. It uses GeoHash indexes to provide spatial queries over data stored in Apache Accumulo. Both HBase and Accumulo are modeled after Google’s BigTable [16], hence, both MD-HBase and GeoMesa are essentially key-value stores with support for spatial operations. As a result, both the design and the objective of the system are very different from an in-memory spatial analytical engine like Simba.

Most existing systems design indexing structures for the MapReduce framework (e.g., Hadoop and HDFS), and they work with indexed data from HDFS. An open source project [2] provides an approach that builds index directly on Spark’s RDD abstraction. However, it only supports one-dimensional ART index [25] on key-value RDDS, which doesn’t extend to spatial query processing.

In addition to system efforts, indexing and query processing for spatial data in MapReduce were explored, for example, $z$-value based indexing [15], range queries and $k$NN queries [12,28,40,40], $k$NN joins [27,39], and spatial join over geometric objects [41]. Various spatial partitioning strategies were explored in MapReduce (using Hadoop). A survey and performance comparison can be found in [19,34]. Simba primarily explored the Sort-Tile-Recursive (STR) partitioning scheme [26] for its indexing module, which has shown to be one of the best spatial partitioning methods (e.g., see latest results in [19]). That said, other spatial partitioning methods can be easily employed and supported by Simba.

Lastly, the general principle of Simba’s query optimizer is no different from those found in classic relational query engines [17], such as selectivity estimation, CBO, and pushing down predicates. But we have to adopt those principles to an in-memory, distributed and parallel environments, and to spatial operations. The cost models developed for partitioning and cost-based spatial query evaluation in the context of Spark are new. Merging and pushing down spatial predicates based on geometric properties in such a distributed and parallel in-memory query engine was also not explored before.

10. CONCLUSION

This paper describes Simba, a distributed in-memory spatial query and analytics engine based on Spark. Simba offers simple and expressive query language in both SQL and DataFrame API. Simba extends Spark SQL with native support to spatial operations, introduces indexes on RDDS, and adds spatial-aware (logical and cost-based) optimizations to select good query plans. Extensive experiments reveal its superior performance compared to other systems.

For future work, we plan to add native support on more geometric objects (e.g., polygons) and spatial operators (e.g., spatial join over polygons), and data in very high dimensions. We will also design more sophisticated CBOs for effective auto-tuning.
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12. REFERENCES


APPENDIX

A. FULL PROGRAMMING INTERFACE

A.1 SQL

Points. Simba introduces the point object inside the Spark SQL engine, through a scala class. Users can use keyword POINT followed by a list of expressions to express multi-dimensional points, where the number of expressions indicates the number of dimensions. For example, we can use Point(x - 1, y * 2) to express a two dimensional point with the value of x = 1 as the first dimension and the value of y = 2 as the second dimension. Note that it is easy to extend Simba with additional spatial and geometric objects by adding more scala classes inside its engine.

Range predicates. Simba supports box range query and circle range query. For a box range query, user uses the following predicate to check if points are inside a bounding box:

\[ p \text{ IN RANGE} (\text{low}, \text{high}) \]

In the predicate above, parameters low, high represent three point objects expressed by the grammar for points described above. Specifically, low indicates an input point for the predicate to check, while high specifies the bounding box (lower-left and higher-right points) for the range query. Points low and high can reside in arbitrary dimensions.

Similarly, user specifies a circle range query as below:

\[ p \text{ IN CIRCLE RANGE} (c, r) \]

Note that p is again an input point for the predicate to check, while the point object c and the constant r indicate a circle centered at point c with radius r which specifies a circle range.

kNN predicates. Similar to the range query predicates, Simba provides the kNN predicate as follows:

\[ p \text{ IN kNN} \]

It checks if p is in the set of k nearest neighbors of a query point q, with respect to an input table. The input table is indicated by the relation after the FROM clause. A kNN predicate is a select condition in the WHERE clause. A kNN predicate can also serve as the join condition for a kNN join operation.
Distance joins. User expresses a distance join between two tables \( R \) and \( S \) with a distance threshold \( \tau \) as follows:

\[
\text{DISTANCE JOIN } S \text{ ON a IN CIRCLE RANGE}(r, \tau)
\]

Here \( s \) (resp. \( r \)) are points built from a record in table \( S \) (resp. \( R \)).

\( k \)NN joins. A \( k \)NN join between table \( R \) and table \( S \) is expressed as follows:

\[
\text{KNN JOIN } S \text{ ON } s \text{ IN KNN}(r, k)
\]

Similar to distance join, \( s \) (resp. \( r \)) are built from a record in \( S \) (resp. \( R \)). User can also invoke approximate \( k \)NN join using ZKJSPPark (Section 6.3.2) by replacing \( \text{KNN JOIN} \) with \( \text{ZKNN JOIN} \).

Index management. Simba allows users to manipulate indexes easily with its index management keywords. Specifically, user is able to create an index through:

\[
\text{CREATE INDEX} \ idx\_name \ ON R(x_1,...,x_m) \ USE \ idx\_type
\]

It builds a new index over \( m \) attributes \( \{x_1,...,x_m\} \) in table \( R \) using a specific index type as indicated by \( \text{idx}\_type \) (which can be R-tree, tree map or hash map). The index is named as \( \text{idx}\_name \). User can show the indexes already built on table \( R \) at anytime:

\[
\text{SHOW INDEX ON } R
\]

In addition, user can drop an index through the index name, or drop all indexes on a table through the table name:

\[
\text{DROP INDEX} \ idx\_name \ ON \ table\_name
\]

Lastly, Simba’s SQL commands are fully integrated with Spark SQL’s SQL query interface. In other words, user can easily use these keywords and commands together with arbitrary SQL predicates from the standard SQL library supported by Spark SQL.

A.2 DataFrame API

Points. Simba also introduces the point object in the DataFrame API, which wraps a list of expressions into a multi-dimensional point that can be processed by Simba’s query engine. For example, we can express a three dimensional point as follows:

\[
\text{Point}(tb(\"x\"), tb(\"y\"), tb(\"z\"))
\]

Specifically, the code above wraps three attributes \( x, y \) and \( z \) from table \( t \) into a point object for further processing.

Single-relation operations. User can apply (box or circle) range queries and \( k \)NN queries directly on data frames. Specifically, in the DataFrame API, Simba provides the following functions:

\[
\text{range(base: Point, low: Point, high: Point)}
\]

\[
\text{circleRange(base: Point, center: Point, r: Double)}
\]

\[
\text{knn(base: Point, q: Point, k: Int)}
\]

In the APIs described above, \( base \) indicates the point objects to be filtered, while the other parameters give filter conditions.

Join operations. In the DataFrame API of Simba, distance joins and \( k \)NN joins can be expressed with following functions:

\[
\text{distanceJoin(target: DataFrame, left_key: Point, right_key: Point, k: Int)}
\]

\[
\text{knnJoin(target: DataFrame, left_key: Point, right_key: Point, k: Int)}
\]

These functions will join the current data frame with another data frame \( target \) using the join condition (either distance join with threshold \( \tau \), or \( k \)NN join with value \( k \)) over \( left\_key \) (a point from the first data frame) and \( right\_key \) (a point from the second data frame).

Index management. User can easily create and drop indexes on an input data frame through:

\[
\text{index(index_type: IndexType, index_name: String, attr: Seq[Attribute])}
\]

\[
\text{dropIndex()}
\]

Finally, note that Simba’s data frame API is integrated with, and can call the data frame API, from Spark SQL, and other spark-based systems that support the data frame API such as MLLib.

A.3 Limitations of the Programming Model

Simba’s main programming and user interface is SQL and the DataFrame API, both of which only provide declarative semantics. As a result, Simba does not have native support for conditional branching (e.g. If...Else), looping (For and While loops), and recursion. That said, because Simba is based on Spark which allows users to develop and submit a customized Java or Scala program for execution, users can always overcome the aforementioned hurdles in Simba through a user program in Java or Scala and submit the program to Simba for execution.

B. RANGE QUERY

Two types of range queries are supported in Simba, namely box and circle range queries. They can be expressed by standard SQL queries in Spark SQL by using filters with properly constructed range conditions. But without Simba’s programming interfaces described in Section 4, the statement becomes clumsy and error-prone. More importantly, without indexes, the engine has to scan all records, which is quite inefficient and resource intensive.

In contrast, Simba allows users to express range queries natively as shown in Section 4, and it can handle range queries using indexes (assuming that the spatial attributes are indexed):

Global filtering. In this step, Simba uses the global index to prune partitions that do not overlap with the query range. In particular, Simba inspects the global index to obtain IDs of the partitions which intersect the query area. Next, Simba calls a Spark internal developer API PartitionPruningRDD, which can filter partitions by ID, to mark required partitions.

Local processing. For each selected partitions from global filtering, Simba uses its local index to quickly return matching records from local data. If \( mbr(R) \) is completely inside the query area, all records in \( R \) can be returned even without checking the index.

C. PROOF OF THEOREM 1

Theorem 1 For any partition \( R_i \) where \( i \in [1, n] \), we have:

\[
\forall r \in R_i, \text{ knn}(r, S) \subseteq \{ s | s \in S, |cr_i, s| \leq \gamma_i \}, \text{ for } \gamma_i \text{ defined in (1)}.
\]

Proof. Recall that \( \text{knn}(cr_i, S') = \{s_1, ..., s_k\} \) (in ascending order of their distances to \( cr_i \)), and \( u_i = \max_{r \in R_i} |r, cr_i| \). Hence, for any \( r \in R_i \), and for any \( t \in [1, k] \), we have:

\[
|r, s_t| \leq |r, cr_i| + |cr_i, s_t| \quad \text{(triangle inequality)}
\]

\[
\leq u_i + |cr_i, s_t|. \quad \text{(by construction)}
\]

This implies that a circle centered at \( r \) with radius \( u_i + |cr_i, s_t| \) will cover at least \( k \) points (i.e., at least \( s_1, s_2, ..., s_k \)) in \( S' \subseteq S \). In other words, \( \text{knn}(r, S) \subseteq S_i = \{ s | s \in S, |r, s| \leq u_i + |cr_i, s_t| \} \). We denote this set as the cover set of record \( r \).

For each element \( e \in S_i \), we have:

\[
|e, cr_i| \leq |e, r| + |r, cr_i| \quad (\forall r \in R_i, \text{triangle inequality})
\]

\[
\leq u_i + |cr_i, s_k| + u_i = \gamma_i,
\]

which implies \( S_i \) is a subset of \( \{ s | s \in S, |cr_i, s| \leq \gamma_i \} \). Thus, \( \forall r \in R_i, \text{ knn}(r, S) \subseteq S_i \subseteq \{ s | s \in S, |cr_i, s| \leq \gamma_i \} \). \hfill \Box

D. ADDITIONAL EXPERIMENTS

D.1 Impact of partition size

Figure 19 shows that Simba’s index construction cost grows roughly linearly with respect to partition size. This is because it is more costly to build local indexes over larger partitions (which outweighs the savings resulted from processing less number of partitions).
Figure 19: Index construction cost: effect of partition size.

Figure 20: Range query performance on OSM: partition size.

Figure 21: kNN query performance on OSM: partition size.

Figure 22: Effect of partition size for join operations.

Figure 23: Range query performance on RC: dimensionality.

Figure 24: kNN query performance on RC: dimensionality.

Figure 25: Comparison between table representations.

**D.2 Influence of Dimensionality on RC**

Figures 23 and 24 show the results for range and kNN queries when dimensionality increases from 2 to 6 on the RC data set. The trends are similar to that on the GEDLT data set as in Figures 16 and 17: Simba significantly outperforms Spark SQL in all dimensions.

**D.3 Impact of the Array Structure**

In this section, we experimentally validated our choice of packing all records in a partition to an array object. Specifically, we compare three different data representation strategies as below:

- **Alternative 1 (A1):** packing all Row objects in a partition into an array.
- **Alternative 2 (A2):** cache RDD[Row] directly.
- **Alternative 3 (A3):** in-memory columnar storage strategy.

We demonstrate their space consumption and scanning time on our default dataset (OSM data with 500 million records) in Figure 25. Note that these records are variable-length records (as each record contains two variable-length string attributes, the two text information fields in OSM).

Figure 25(a) shows the space consumption of different strategies. Packing all Row objects within a partition to an array object (A1 in Figure 25) consumes slightly more space than directly caching the RDD[Row] in Spark SQL (A2 in Figure 25). Such overhead is caused by additional meta information kept in array objects. On the other hand, the in-memory columnar storage (A3 in Figure 25) clearly saves space due to its columnar storage with compression.

The table scan time is shown in Figure 25(b). Caching RDD[Row] directly shows the best performance. The array structure adopted by Simba has slightly longer scanning time, due to the small space overhead and the additional overhead from flattening members out of the array objects. Lastly, the in-memory columnar storage gives the worst performance since it requires joining multiple attributes to restore the original Row object (and the potential overhead from decompression), whose overhead outweighs the savings resulted from its less memory footprint.

That said, Simba can also choose to use the in-memory columnar storage (and with compression) to represent its data.